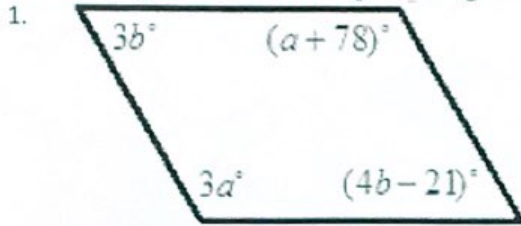


Properties of Parallelograms

Given the quadrilateral is a parallelogram, find the value of the variable(s).

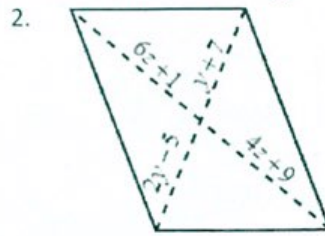


$$\begin{aligned} 3b &= 4b - 21 \\ -4b & \quad -4b \\ -b &= -21 \end{aligned}$$

$$\boxed{b = 21}$$

$$\begin{aligned} 3a &= a + 78 \\ -a & \quad -a \\ 2a &= 78 \\ \frac{2a}{2} & \quad \frac{78}{2} \end{aligned}$$

$$\boxed{a = 39}$$

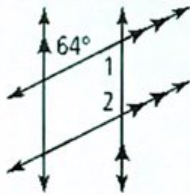


$$\begin{aligned} 6z + 1 &= 4z + 9 \\ 2z &= 8 \\ \boxed{z} &= \boxed{4} \end{aligned}$$

$$\begin{aligned} 2y - 5 &= y + 7 \\ \boxed{y} &= \boxed{12} \end{aligned}$$

Review Problems:

3. Find the $m\angle 1$ and $m\angle 2$. Justify your answer.



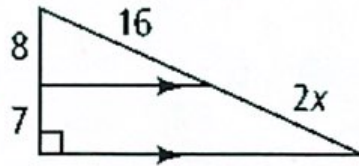
Alternate Interior \angle s

$$\angle 1 = 64^\circ$$

$$\angle 2 = 180 - 64 = 116^\circ$$

$$\boxed{\begin{aligned} \angle 1 &= 64^\circ \\ \angle 2 &= 116^\circ \end{aligned}}$$

4. Solve for x.



$$\frac{8}{7} = \frac{16}{2x}$$

$$16x = 112$$

$$\boxed{x = 7}$$

5. Solve for x.



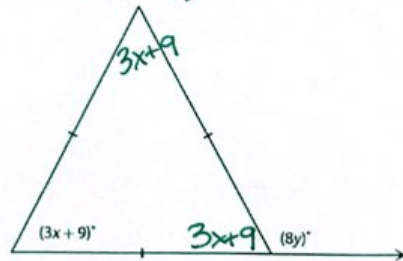
$$\frac{6}{9} = \frac{x-4}{x}$$

$$\begin{aligned} 6x &= 9x - 36 \\ -9x & \quad -9x \end{aligned}$$

$$-3x = -36$$

$$\boxed{x = 12}$$

6. Solve for x and y.



$$3x + 9 + 3x + 9 + 3x + 9 = 180$$

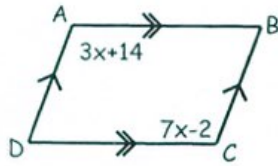
$$9x + 27 = 180$$

$$9x = 153$$

$$\boxed{x = 17}$$

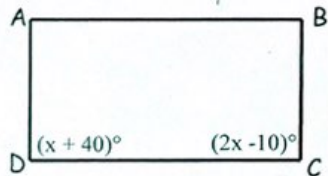
Construct a proof for each problem

7. Given: $\square ABCD$ is a parallelogram,
Prove: $x = 4$



Statement	Reason
1. $\square ABCD$	1. Given
2. $\angle A \cong \angle C$	2. Opposite sides of \square are congruent
3. $3x+14 = 7x-2$	3. Substitution
4. $14 = 4x-2$	4. Subtraction
5. $16 = 4x$	5. Addition
6. $x = 4$	6. Substitution

8. Given: $\square ABCD$ is a rectangle,
Prove: $x = 50$



Statement	Reason
1. $\square ABCD$ is a rectangle	1. Given
2. $\angle D \cong \angle C$	2. Same Side interior theorem
3. $x+40 = 2x-10$	3. Substitution
4. $x+50 = 2x$	4. Addition
5. $50 = x$	5. subtraction