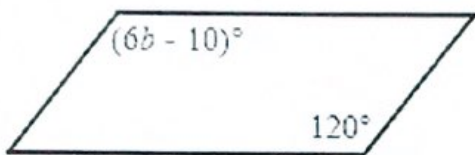


What would the value of the variable need to be in order for the quadrilateral to be a parallelogram?

1.



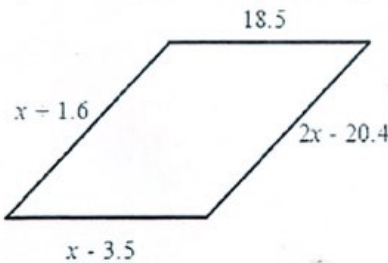
$$6b - 10 = 120$$

$$+10 \quad +10$$

$$\frac{6b}{6} = \frac{130}{6}$$

$$b = 21.\bar{6}$$

2.

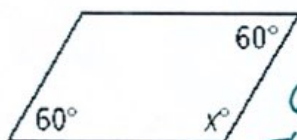


$$x - 3.5 = 18.5$$

$$+3.5 \quad +3.5$$

$$x = 22$$

3.

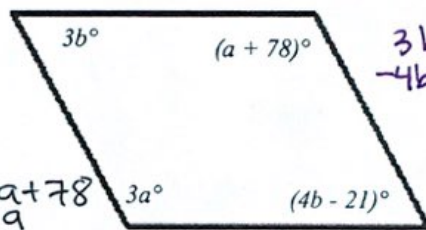


$$60 + x = 180$$

$$-60 \quad -60$$

$$x = 120$$

4.



$$3b = 4b - 21$$

$$-4b \quad -4b$$

$$-b = -21$$

$$\frac{-b}{-1} = \frac{-21}{-1}$$

$$b = 21$$

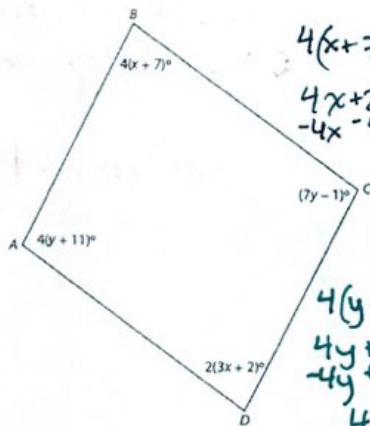
$$3a = a + 78$$

$$-a \quad -a$$

$$\frac{2a}{2} = \frac{78}{2}$$

$$a = 39$$

5.



$$4(x + 7) = 2(3x + 2)$$

$$4x + 28 = 6x + 4$$

$$-4x \quad -4 \quad -4x \quad -4$$

$$\frac{24}{2} = \frac{2x}{2}$$

$$x = 12$$

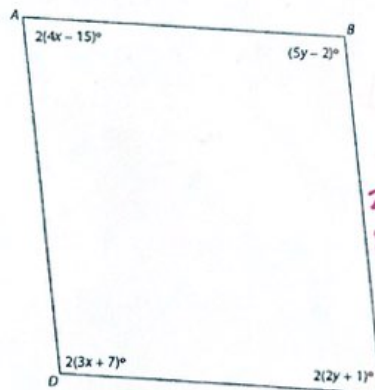
$$4(y + 11) = 7y - 1$$

$$4y + 44 = 7y - 1$$

$$-4y \quad +1 \quad -4y \quad +1$$

$$\frac{45}{3} = \frac{3y}{3}$$

$$15 = y$$



$$2(4x - 15) + 2(3x + 7) = 180$$

$$8x - 30 + 6x + 14 = 180$$

$$14x - 16 = 180$$

$$+16 \quad +16$$

$$\frac{14x}{14} = \frac{196}{14}$$

$$x = 14$$

$$2(2y + 1) + 5y - 2 = 180$$

$$4y + 2 + 5y - 2 = 180$$

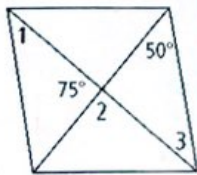
$$9y = 180$$

$$\frac{9y}{9} = \frac{180}{9}$$

$$y = 20$$

Find the measure of the numbered angles for each parallelogram.

7.



$$180 - 75 = 105 = \angle 2$$

$$105 = 50 + \angle 3$$

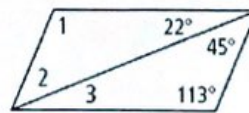
$$-50 \quad -50$$

$$55 = \angle 3$$

$$\angle 1 = 55$$

ext. angle theorem

8.



$$\angle 1 = 113$$

$$\angle 2 = 45$$

$$\angle 3 = 22$$

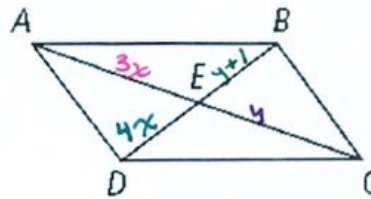
□ABCD is a parallelogram. Find the value of x and y and the length of each diagonal.

9. $AE = 3x$, $EC = y$, $DE = 4x$, $EB = y + 1$

$3x = y$ $4x = y + 1$

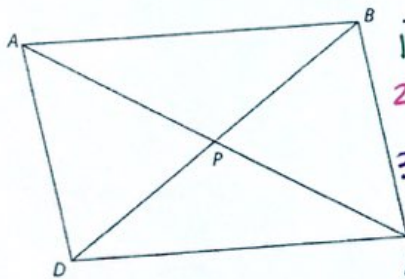
$4x = 3x + 1$
 $-3x \quad -3x$
 $x = 1$

$3(1) = y$
 $3 = y$



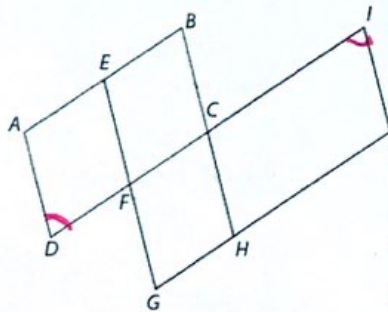
Proofs: Construct a proof for the following problems.

10. Given that □ABCD is a parallelogram, prove that $\triangle DPA \cong \triangle BPC$



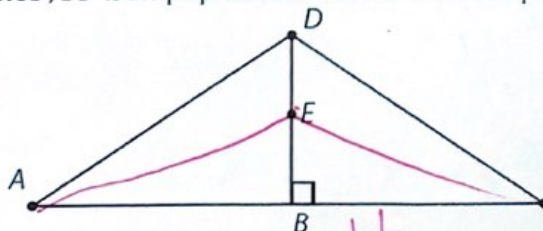
Statement	Reason
1. □ABCD is a parallelogram	1. Given
2. $\overline{AD} \cong \overline{BC}$	2. opposite sides of a parallelogram are congruent
3. $\overline{DP} \cong \overline{PB}$ and $\overline{AP} \cong \overline{PC}$	3. Diagonals of a parallelogram bisect each other
4. $\triangle DPA \cong \triangle BPC$	4. SSS Triangle Congruence

11. Given that □ABCD, □EBHG, and □FIJG are parallelograms, prove that $\angle D \cong \angle I$



Statement	Reason
1. □ABCD, □EBHG, □FIJG are parallelograms	1. Given
2. $\angle D \cong \angle B$	2. Opposite \angle 's of a \square are congruent
3. $\angle B \cong \angle G$	3. " "
4. $\angle G \cong \angle I$	4. " "
5. $\angle D \cong \angle I$	5. Substitution.

12. Prove that a point on a perpendicular bisector is equidistant from the endpoints of the segment it bisects given that in $\triangle ACD$, \overline{BD} is the perpendicular bisector of \overline{AC} and point E is on \overline{BD} . Write your answer in a proof.



Given:
 \overline{DB} is the perpendicular bisector of \overline{AC} .
 E is a point on \overline{DB} .

Prove:
 $EA = EC$

Statement	Reason
1. \overline{DB} is the perpendicular bisector of \overline{AC}	1. Given
2. Draw \overline{EA} and \overline{EC}	2. Construction
3. $AB \cong BC$	3. Definition of Bisector
4. $EB \cong BE$	4. Reflexive Property
5. $\angle ABE = 90 = \angle CBE$	5. Perpendicular
6. $\triangle ABE \cong \triangle CBE$	6. SAS
7. $EA \cong EC$	7. CPCTC

NOT ENOUGH ROOM!!